

Physics 8 — Friday, December 6, 2019

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We often write $x(t)$ in terms of $\omega =$ “natural angular frequency:”

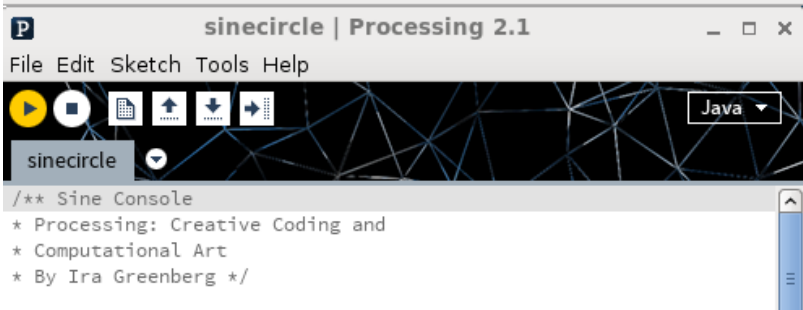
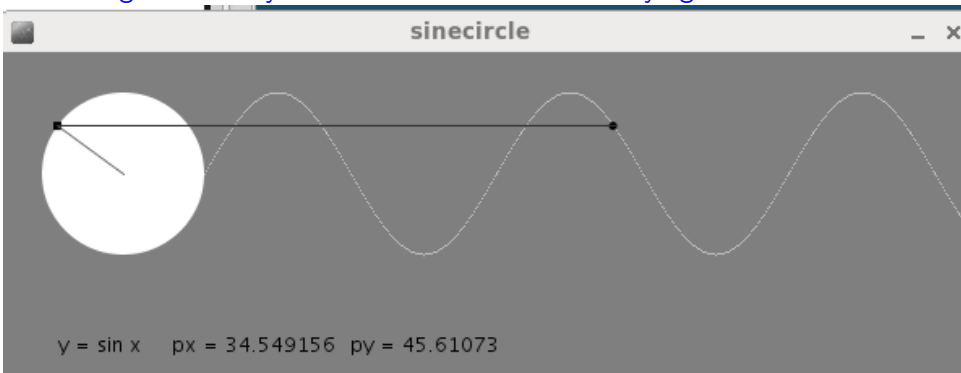
$$x = A \cos(\omega t + \phi_i)$$

but we can equivalently use $f =$ “natural frequency:”

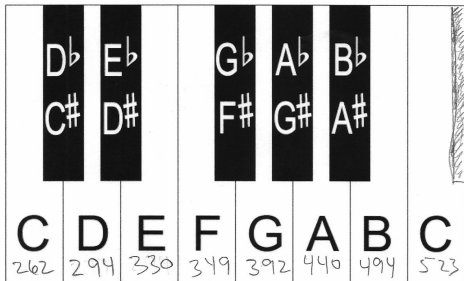
$$x = A \cos(2\pi f t + \phi_i)$$

- ▶ $f =$ *frequency*, measured in cycles/sec, or Hz (hertz)
- ▶ $\omega = \frac{f}{2\pi}$ is *angular frequency*, measured in radians/sec, or s^{-1}
- ▶ The frequency $f = 2\pi\omega$ is much more intuitive than ω
- ▶ Using ω keeps the equations cleaner — can be helpful for derivations, etc., so that you don't have to keep writing 2π

“angular velocity” ω is our old friend from studying circular motion:



"frequency" $f = \frac{\omega}{2\pi}$ is more familiar from music, etc.



$$(\sqrt[12]{2})^4 = 1.2599 \approx \frac{5}{4} \text{ (major 3rd)}$$

$$(\sqrt[12]{2})^5 = 1.3348 \approx \frac{4}{3} \text{ (perfect 4th)}$$

$$(\sqrt[12]{2})^7 = 1.4984 \approx \frac{3}{2} \text{ (perfect 5th)}$$

$$(\sqrt[12]{2})^{12} = 2 \text{ (an octave!)}$$

- ▶ A above middle C: 440 Hz
- ▶ Middle C: 261.63 Hz
- ▶ $440 \times (\frac{1}{2})^{\frac{3}{4}} = 261.63$
- ▶ Octave = factor of 2 in frequency f
- ▶ Half step = factor of $\sqrt[12]{2}$ in frequency
- ▶ Whole step = factor of $\sqrt[6]{2}$ in frequency
- ▶ Major scale (white keys, starting from C) = (root) W W H W W W H
- ▶ Minor scale (white keys, starting from A) = (root) W H W W H W W

Let's return to our two favorite examples of oscillating systems.

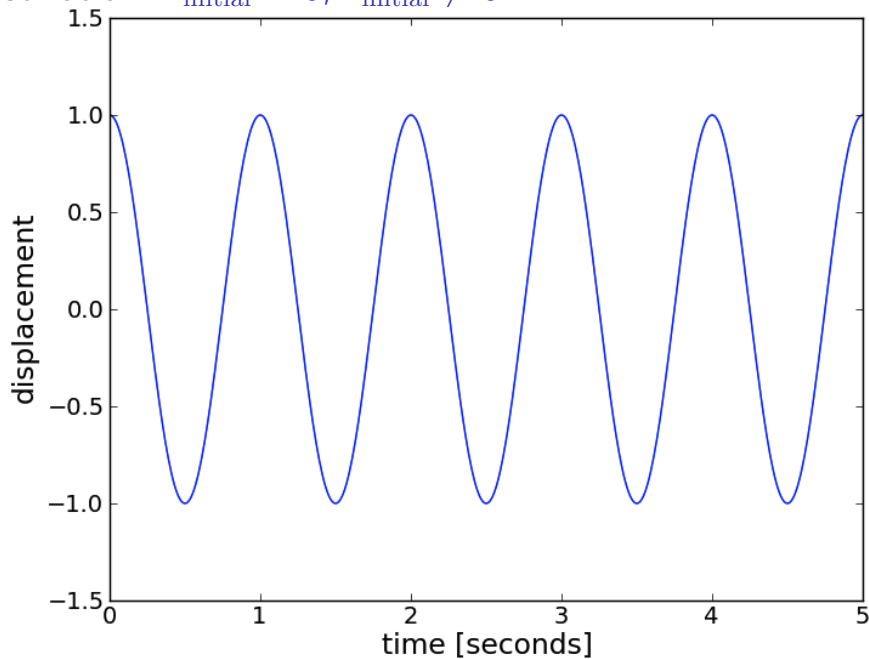
Natural frequency & period for mass on spring:

$$f_0 = \frac{1}{2\pi} \sqrt{\frac{k}{m}} \qquad T_0 = 2\pi \sqrt{\frac{m}{k}}$$

Natural frequency & period for simple pendulum (small heavy object at end of “massless” cable):

$$f_0 = \frac{1}{2\pi} \sqrt{\frac{g}{\ell}} \qquad T_0 = 2\pi \sqrt{\frac{\ell}{g}}$$

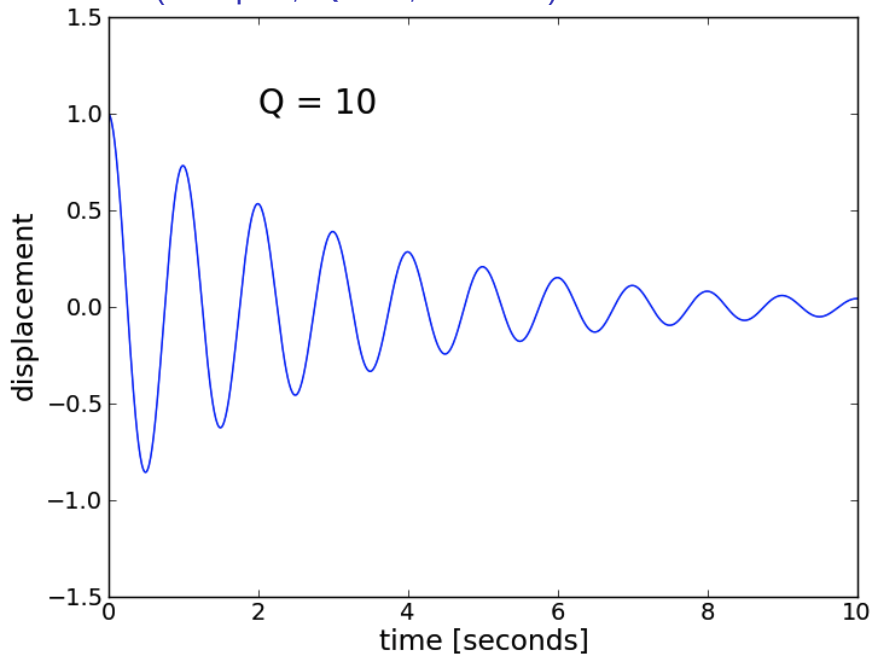
Oscillation: $v_{\text{initial}} = 0$, $x_{\text{initial}} \neq 0$



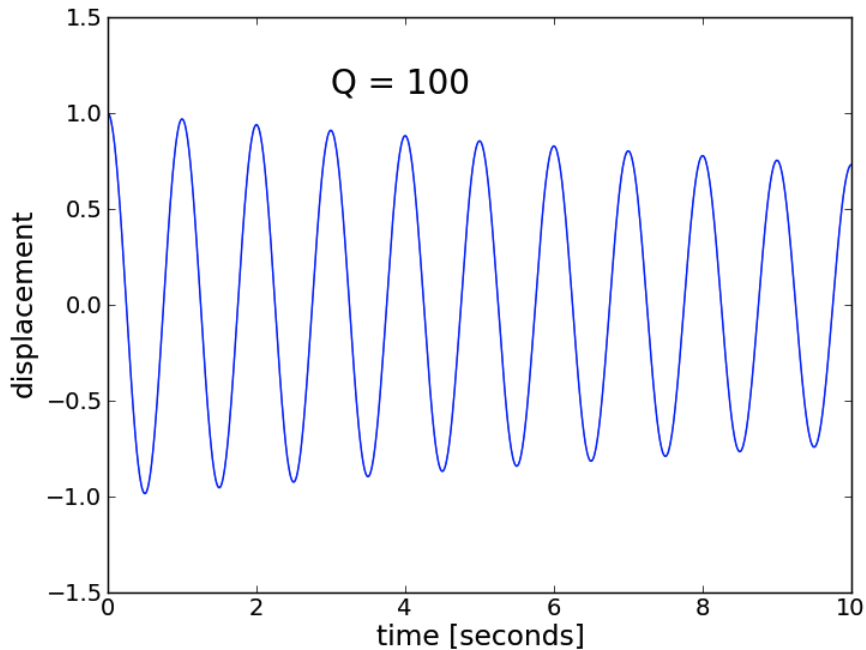
Missing from previous picture: **damping**

- ▶ Without some kind of external push, a swingset eventually slows to a stop, right? Eventually the mechanical energy is dissipated by friction, air resistance, etc.
- ▶ A piano wire doesn't vibrate forever, does it?
- ▶ Normally once you hit a key, the sound dies out after about half a second or so.
- ▶ If your foot is on the sustain pedal, the sound lasts several seconds.
- ▶ What is the difference?
- ▶ It's the felt *damper* touching the strings!

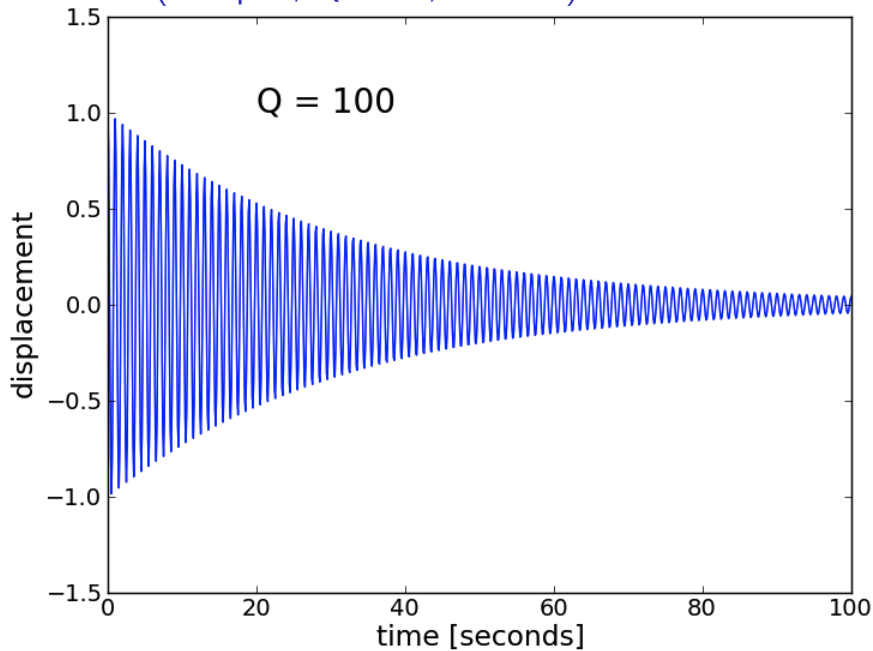
Oscillation (damped, $Q=10$, $f=1$ Hz)



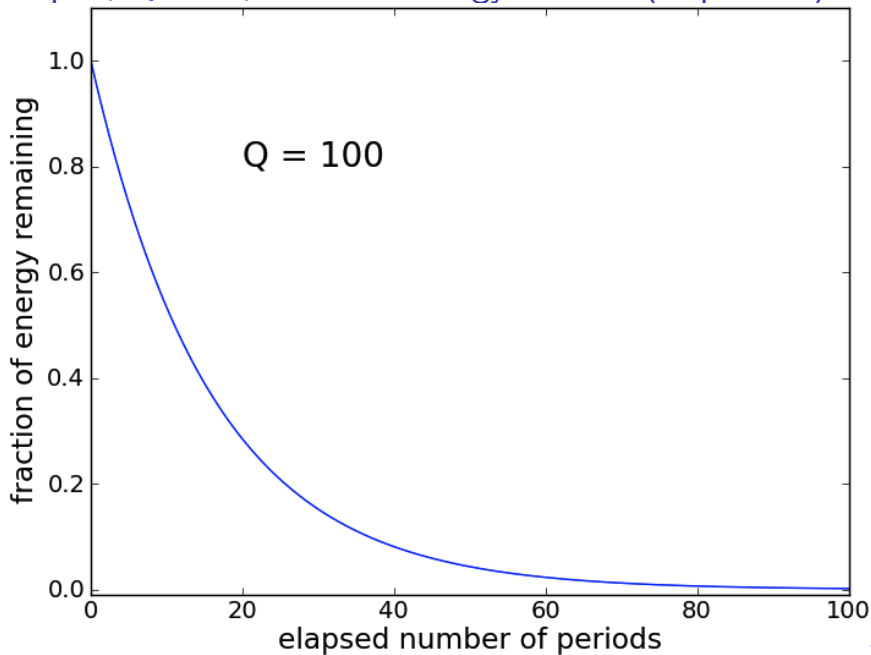
Oscillation (damped, $Q=100$, $f=1$ Hz)



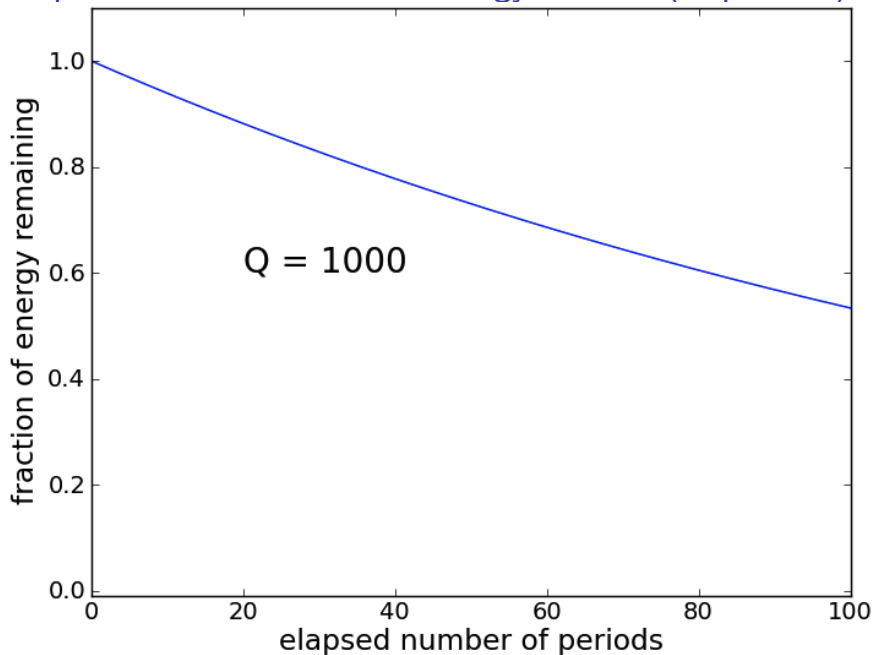
Oscillation (damped, $Q=100$, $f=1$ Hz)



Damped, $Q=100$, $f=1$ Hz: energy vs time (in periods)



Damped, $Q=1000$, $f=1$ Hz: energy vs time (in periods)



For a given frequency f ,

- ▶ Less damping \leftrightarrow higher Q
- ▶ More damping \leftrightarrow lower Q
- ▶ $Q = \omega\tau$ is number of radians after which energy has decreased by a factor $e^{-1} \approx 0.37$
- ▶ Equivalently, $Q = 2\pi f\tau$ is number of cycles after which energy has decreased by a factor $e^{-2\pi} \approx 0.002$
- ▶ More simply, Q is roughly the number of periods after which nearly all of the energy has been dissipated.
- ▶ “Tinny” sound of frying pan \leftrightarrow low Q (fast dissipation)
- ▶ Smooth, enduring sound of a gong, or a bell tower \leftrightarrow high Q (slow dissipation)

Suppose you want to go for a long time on a swing set.

Dissipation is continuously removing energy.

If you're going to keep going for many minutes, you need some way of continuously putting energy back in.

If you're a big kid, you swing your feet. If you're a little kid, your parent or older sibling pushes you.

The push of parent or swing of feet has to be at approximately the natural frequency of the swingset, or else you don't get anywhere!

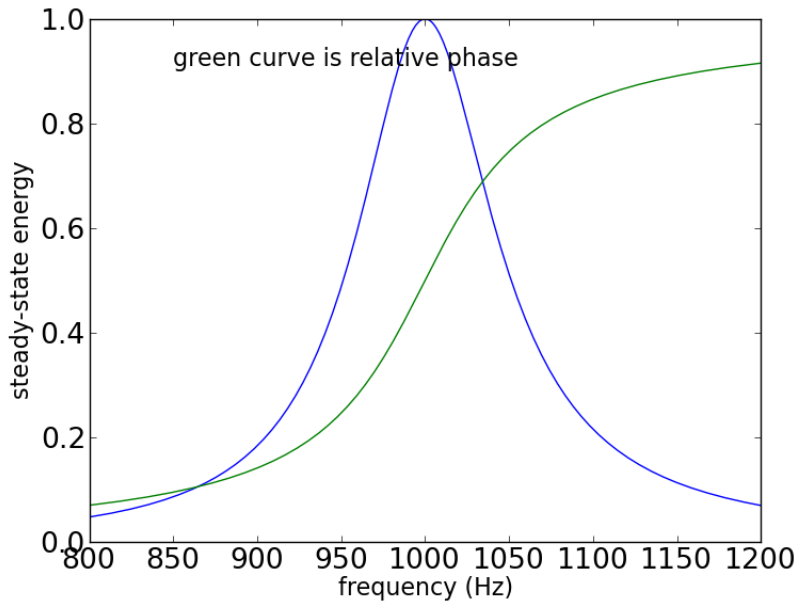
But if your pushes are close to the right interval, the amplitude gets larger and larger with each successive push, until eventually the rate at which the push is adding energy equals the rate at which dissipation is removing energy.

Hitting the right frequency is called resonance

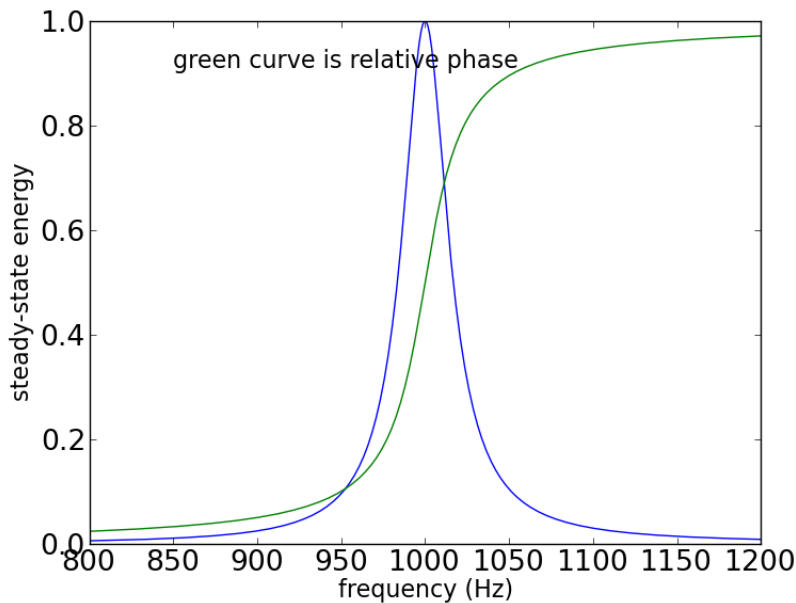
The higher the Q (i.e. slower dissipation), the more periods you have available for building up energy. A high Q makes it easy to build up a really big amplitude!

But the higher the Q , the closer you have to get to the right frequency in order to get the thing moving.

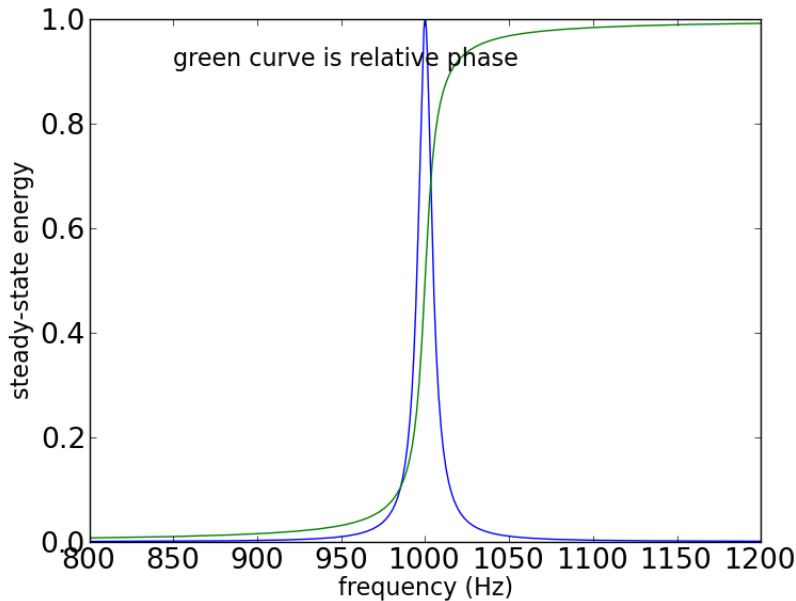
$f_0 = 1000$ Hz, $Q = 10$: energy and phase vs. f_{push}



$f_0 = 1000$ Hz, $Q = 30$: energy and phase vs. f_{push}



$f_0 = 1000$ Hz, $Q = 100$: energy and phase vs. f_{push}



(avoiding) resonance in structures

<https://99percentinvisible.org/episode/supertall-101/>

(avoiding) resonance in structures

Lateral Loads and Stability

Natural period of oscillation

- harmonic motion
- period of a structure is proportional to weight and inversely proportional to stiffness

Lateral stability of structures

- braced frame
- rigid frame
- shear wall

Code and Safety in Design

- factor of safety
- resilience

Design strategies

- absorb energy in the structure (flexible joints, shock absorbers)
(example Bell Atlantic, west coast buildings)
- tuned mass dampers (CitiGorp)
- building shape (Burj Khalifa)

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